POSSIBLE CHROMOSPHERIC ACTIVITY CYCLES IN AD LEO

ANDREA P. BUCCINO^{1,2,4}, ROMINA PETRUCCI^{1,4}, EMILIANO JOFRÉ^{3,4}, AND PABLO J. D. MAUAS^{1,2,4}

¹ Instituto de Astronomía y Física del Espacio (CONICET-UBA), C.C. 67 Sucursal 28, C1428EHA-Buenos Aires, Argentina

² Departamento de Física, FCEN-Universidad de Buenos Aires, Buenos Aires, Argentina

³ Observatorio Astronómico de Córdoba, Córdoba, Argentina

Received 2013 October 13; accepted 2013 December 10; published 2013 December 23

ABSTRACT

AD Leo (GJ 388) is an active dM3 flare star that has been extensively observed both in the quiescent and flaring states. Since this active star is near the fully convective boundary, studying its long-term chromospheric activity in detail could be an appreciable contribution to dynamo theory. Here, using the Lomb–Scargle periodogram, we analyze the Ca II K line-core fluxes derived from CASLEO spectra obtained between 2001 and 2013 and the V magnitude from the ASAS database between 2004 and 2010. From both of these totally independent time series, we obtain a possible activity cycle with a period of approximately seven years and a less significant shorter cycle of approximately two years. A tentative interpretation is that a dynamo operating near the surface could be generating the longer cycle, while a second dynamo operating in the deep convection zone could be responsible for the shorter one. Based on the long duration of our observing program at CASLEO and the fact that we observe different spectral features simultaneously, we also analyze the relation between simultaneous measurements of the Na I index (R'_D) , H α , and Ca II K fluxes at different activity levels of AD Leo, including flares.

Key words: stars: activity - stars: flare - stars: low-mass

Online-only material: color figures

1. INTRODUCTION

Activity cycles like that observed in the Sun have been detected in several late-type stars (e.g., Baliunas et al. 1995; Buccino & Mauas 2008). The usually accepted model to describe the generation and intensification of magnetic fields in these stars is the $\alpha\Omega$ -dynamo first invoked to explain solar activity (Parker 1955) which has been thoroughly improved and extended from F to early M stars (e.g., Robinson & Durney 1982; Saar & Brandenburg 1999; Lorente & Montesinos 2005). These dynamo models are based on the interaction between differential rotation (the Ω -effect) and convective turbulence (the α -effect) in the tachocline.

Cool stars with masses lower than about $0.35 M_{\odot}$ are believed to be fully convective (Chabrier & Baraffe 1997). Therefore, they do not possess a tachocline and could not support an $\alpha\Omega$ dynamo. Nevertheless, there is plenty of observational evidence that slow late-type rotators like dMe stars are very active and have strong magnetic fields (Hawley 1989; West et al. 2004; Reiners & Basri 2007). Chabrier & Küker (2006) proposed that a pure α^2 -dynamo could generate large-scale magnetic fields in fully convective stars. Moreover, the three-dimensional dynamo model developed by Browning (2008) for M dwarfs reveals that fully convective stars can generate kG-strength magnetic fields without the aid of a shearing tachocline.

To determine whether there is an onset of cyclic activity near the convective limit, it is of special interest to study the long-term chromospheric activity in stars of different spectral types, in particular in middle-M stars. As a contribution to this subject, since 1999 we have developed the HK α Project, an observing program dedicated to periodically obtaining midresolution echelle spectra of southern late-type stars, including fully convective ones. From our data, we found evidence of cyclic activity for the fully convective M5.5Ve star Proxima Centauri (Cincunegui et al. 2007b), for the mid-M spectroscopic binary GJ 375 (Díaz et al. 2007b), and the two early M stars GJ 229 A and GJ 752 A (Buccino et al. 2011). Similarly, Gomes da Silva et al. (2012) studied a sample of stars from the *HARPS* program and found that the long-term activity of eight early M stars can be fitted by a sinusoidal signal.

One of the most observed stars of our sample is AD Leo (GJ 388), which is a M3Ve star (Henry et al. 1994), wellknown for its frequent (Pettersen et al. 1984; Crespo-Chacón et al. 2006) and strong flares (e.g., Hawley & Pettersen 1991). Flares in AD Leo have been observed and studied in the optical, EUV, and X-ray (e.g., Hawley et al. 1995; Mauas & Falchi 1996; Favata et al. 2000; Hawley et al. 2003; Güdel et al. 2003). Recently, Hunt-Walker et al. (2012) obtained a rotational period, $P_{\rm rot}$, of 2.23 days for this star. AD Leo is a partially convective star of mass $\sim 0.40 M_{\odot}$ (Favata et al. 2000). Morin et al. (2008) found that AD Leo hosts a magnetic field with similar properties to several fully convective stars. Although it has been extensively observed both in the quiescent and flaring states, most analyses of the chromospheric activity in AD Leo are related to its shortterm variability. Only Pettersen et al. (1986) reported long-term variations in its flare frequency and suggested a cycle in flaring activity.

This active fast-rotator star is an interesting target to explore the dynamo around the threshold for full convection. Here we present a detailed study of its long-term chromospheric activity. We delineate in Section 2 the main characteristics of the HK α Project and the All Sky Automated Survey⁵ (ASAS) program. In section Section 3 we report our results and analyze the Complejo Astronómico El Leoncito (CASLEO) activity indicators and the long-term magnetic activity derived from CASLEO data and the ASAS database. Finally, we discuss our results in the context of dynamo theory.

⁴ Visiting Astronomer, Complejo Astronómico El Leoncito operated under agreement between the Consejo Nacional de Investigaciones Científicas y Técnicas de la República Argentina and the National Universities of La Plata, Córdoba and San Juan.

⁵ http://www.astrouw.edu.pl/asas/

2. OBSERVATIONS

To study the long-term chromospheric activity in late-type stars, in 1999 we started the HK α Project. In this program, we systematically obtain mid-resolution echelle spectra ($R = \lambda/\delta\lambda \approx 26,000$) of several late-type stars. Our observations are made at the 2.15 m telescope of CASLEO, in San Juan, Argentina. Specific details of the observations and the method used to calibrate the spectra are described in Cincunegui & Mauas (2004).

Our stellar sample was chosen to cover the spectral range from F to M, with different activity levels. In particular, we included a large number of M stars to study the transition to the completely convective regime. Most of the stars are single dwarfs, although we also include several binaries and a few subgiants. At present, we have about 5500 spectra of 150 stars.

The standard activity indicator used in dF to dK stars is the Mount Wilson *S* index, essentially the ratio of the Ca II H and K line-core fluxes to the continuum nearby. However, as explained in detail in Buccino et al. (2011), it is not suitable for studying the chromospheric activity on AD Leo. Following our previous works (Díaz et al. 2007b; Buccino et al. 2011), we use as a proxy of stellar activity the Ca II K line-core flux, integrated with a triangular profile of 1.09 Å FWHM centered in 3933.66 Å (Cincunegui et al. 2007a).

We complement our data with photometry from ASAS. The ASAS program systematically observes around 10^7 stars brighter than V = 14, in both the V and I bands simultaneously. Here we use the V magnitude to analyze the long-term activity of AD Leo.

3. RESULTS

3.1. Chromospheric activity cycles

In Table 1 we show the observation logs of AD Leo at CASLEO. There is a total of 38 individual observations, which have been carried out on 19 nights distributed over twelve years between 2001 March and 2013 March. Our observations consist of two successive spectra in order to eliminate cosmic rays. Observation times are between 30 and 60 minutes.

Crespo-Chacón et al. (2006) observed a large number of short and weak flares occurring very frequently (flare activity >0.71 hr⁻¹), which can mask the variations of activity due to the cycle. Therefore, before exploring the existence of an activity cycle in this star, we filter out any flares from our observations. We do this by visual inspection of the observations, since during flares the line fluxes in the two successive spectra are very different. We excluded these flaring spectra, which are indicated in Table 1 with a " \star ," from the rest of the analysis.

For the non-flaring CASLEO spectra, we calculated a nightly average for the Ca II K fluxes. We plot the resulting time series of these activity indicators in Figure 1(a). In this figure we observe that AD Leo reaches its minimum of activity (40% lower than at the maximum) in the year 2007.

On the other hand, we obtained the V magnitude of AD Leo from the ASAS catalog for the period between 2004 and 2010. We only included the best quality data (see Buccino et al. 2011) and we discarded 14 outlier observations. In Figure 1(b) we plot the resulting time series, which consists of 175 points. Typical errors are around 30 mmag. The mean magnitude of the whole data set is around $\langle V \rangle = 9.327 \pm 0.021$. We also look for evidence of rotational modulation due to spots and active regions on the stellar surface, probably responsible for the short-scale variations (~0.5%). To do so, we analyzed the data

 Table 1

 Logs of the CASLEO Observations of AD Leo

Label ^a	xJD ^b	ť
0301c1	1974.57	2700
0301c2	1974.61	2700
*1201c1	2247.82	1800
1201c2	2247.84	1800
0302a1	2363.61	1800
0302a2	2363.63	1800
0303a1	2713.63	3000
0303a2	2713.66	3000
1203b1	2980.82	1800
1203b2	2980.84	1800
0304a1	3072.62	3000
0304a2	3072.66	3000
0604b1	3159.47	1800
★0604b2	3159.49	1800
1104d1	3335.82	1800
1104d2	3335.84	1800
★0305a1	3448.64	1800
★0305a2	3448.67	1800
1206d1	4081.83	2400
1206d2	2980.86	2400
0307a1	4162.69	3600
0307a2	4162.73	3600
0308b1	4547.64	3600
0308b2	4547.68	3600
1208c1	4821.77	3600
1208c2	4821.82	3600
★0309b1	4902.63	3600
0310b1	5262.58	3600
0310b2	5262.62	3600
1210c1	5547.77	2700
1210c2	5547.81	2700
1212b1	6281.82	1800
1212b2	6281.84	1800
★0313b1	6354.64	2850
★0313b2	6354.67	2850

Notes. Spectra indicated with \star are discarded in Figure 1(a) due to the presence of flares.

^a Label built with month and year of the observation (e.g., 0305 refers to 2005 March), a letter for different nights of the same run and a number for each individual nightly spectrum.

^b xJD=JD-2450000, where JD is the Julian date when the observation begins.

^c Exposure time in seconds.

of each observing season with the Lomb–Scargle periodogram (Horne & Baliunas 1986). Nevertheless, we did not detect any significant periodicity in the ASAS seasonal data sets, probably due to the low-precision of the ASAS photometry.

To search for long-term chromospheric activity cycles, we first analyzed both independent data sets with the Lomb–Scargle periodogram. The False Alarm Probabilities (FAPs) of the periods obtained were computed with a Monte Carlo simulation, described in Buccino & Mauas (2009). The periodogram obtained for the CASLEO data is plotted in Figure 2(a) with a dashed line. It shows a primary periodicity in the Ca II K fluxes with a period $P_{1,CASLEO} = (2769 \pm 106)$ days with FAP = 8%, and a second, less significant, harmonic component with period $P_{2,CASLEO} = (842 \pm 9)$ days with FAP = 30%. To analyze the robustness of our results, we computed the periodograms of the series obtained by eliminating each data point alternately. In eleven of fourteen periodograms we obtained $P_{1,CASLEO}$



Figure 1. (a) Ca II K fluxes derived from the non-flaring CASLEO spectra, assuming errors of 10% (Cincunegui & Mauas 2004). The solid line is the least-square fit with a harmonic function of period 2769 days, the most significant peak in Figure 2(a), with $\chi_r = 0.78$. The dashed lines represent $\pm 1\sigma$ deviations. The red circles indicate those points associated with high activity, with a mean higher than 0.5σ . Removing the outlier points (double circled), which might be affected by weak flares, we obtain $P_{1,CASLEO} = 2793$ days with a better FAP = 0.3%. (b) *V* magnitude measured by ASAS. The solid line is the least-square fit with a harmonic curve of period 2659 days ($\chi_r = 0.49$), as obtained in Figure 2(a). The dashed lines represent those points which apart in 1σ from this fit. The monthly means are indicated by square points.

(A color version of this figure is available in the online journal.)



Figure 2. (a) Lomb–Scargle periodogram of the Ca II K fluxes (dashed) and the V magnitude (solid). We represent the error interval of each period with vertical solid and dashed lines. (b) The Ca II K fluxes plotted in Figure 1(a) (dashed) and the quarterly weighted mean V magnitude obtained from the data plotted in Figure 1(b) (solid). Typical errors are $\sim 10\%$ for the Ca II K fluxes and < 0.12% for the mean V magnitudes. For clarity, we do not include the error bars. (A color version of this figure is available in the online journal.)

between 2593 and 2982 days with FAPs < 30% (73% of them were $P_{1,CASLEO} = 2769$ days) and a secondary peak $P_{2,CASLEO}$ between 843 and 931 days with larger FAPs.

To investigate whether the 842 day period is a subharmonic frequency of the prominent peak, we used the monthly sunspot numbers (S_N) taken from the National Geophysical Data Center⁶

to take into account that activity does not follow a strictly sinusoidal law. We used S_N between 1751 and 2012 and rescaled the series in time to the period P = 2769 days (~ 7.58 yr). We also rescaled the S_N to obtain a time series of the same mean value and standard deviation as our data. To consider data with the same signal-to-noise as ours, we added Gaussian noise with errors of 10% at each point. We took 1000 samples of these data with random starting dates and the same phase intervals

⁶ http://www.ngdc.noaa.gov/stp/solar/ssndata.html



Figure 3. Simultaneous measurements of the Na I index R'_D (a) and the H α line-core flux (b) vs. the Ca II K fluxes from CASLEO spectra. The red circles indicate those points where the level of activity exceeds the mean by more than 0.5σ , and the triangles signal those points associated with flares. (A color version of this figure is available in the online journal.)

that we have in our data and we computed the periodograms. As expected, 55% of the most significant periods detected in each periodogram apart from P = 2769 days in less than 10%. On the other hand, only 0.3% are between 671 and 1007 days (842 days \pm 20%). Therefore, we can conclude that the peak at $P_{2,CASLEO} = 842$ days (~2.3 yr) is not an artifact. We also performed a similar analysis on a sinusoidal function of period 2769 days with 10%-Gaussian noise. While 82% of the periods detected are 2769 days ($\pm 10\%$), periods near $P_{2,CASLEO}$ were not detected. This analysis confirms that this secondary peak is not due to aliasing.

In Figure 2(a) we show the periodogram for the ASAS time series. We obtained prominent peaks at $P_{1,ASAS} = (2569 \pm$ 107) days (FAP $\sim 10^{-12}$) and $P_{2,ASAS} = (867 \pm 6)$ days (FAP \sim 10^{-9}). Since the ASAS data timespan is only ~4.5 years, periods longer than P_1 are also potentially significant, as indicated by high periodogram power (Figure 2(a)). The large number of points of this series are responsible for these extremely low FAPs (see Horne & Baliunas 1986, Equation (22)). To check that these periods are significantly independent of the data dimensions, we reduce the number of points by binning the data. We computed the monthly mean V magnitude (i.e., averaging on timescales much longer than $P_{\rm rot}$), weighted by the error reported in the ASAS database, and we computed the error of each mean magnitude as the square root of the variance-weighted mean (see Frodesen et al. 1979, Equation (9.12)). For this series we detected a period $P_{ASAS} = (2937 \pm 575)$ days, with a FAP = 10^{-5} . Since we smoothed the data plotted in Figure 1(b), the secondary period near ~900 days is much less significant (FAP = 5%) in this periodogram.

The CaII K fluxes and the mean quarterly magnitudes are plotted together in Figure 2(b). Contrary to the Sun, we observe that spots dominate the emission in AD Leo as it becomes fainter when the CaII emission increases. On the other hand, there is an evident time lag between both chromospheric series. Both data sets coincide within the normalization constant with a correlation coefficient R = 0.95, if we shift the photometry by 770 days.

Gray & Baliunas (1995) and Gray et al. (1996a, 1996b) have already observed this time lag between photometric and magnetic variations for stars of different spectral types (G0V-K2V). Gray et al. (1996a) showed that, when different stars are compared, this time lag is anti-correlated with effective temperature. However, the Sun does not fit this relation (Gray & Livingston 1997). Furthermore, here we find that AD Leo does not follow this trend, similarly to what we found for other M stars (Díaz et al. 2007b; Buccino et al. 2011). The physical explanation for these time lags remains unknown (Brown et al. 2008).

3.2. H α and Na I D lines as activity indicators

Due to both their red color and faint intrinsical luminosity, it is quite difficult to observe the CaII lines in dM stars with adequate signal-to-noise, especially for programs aiming to follow a large number of stars. Therefore, it would be very convenient to find other activity indicators at longer wavelengths. Since we observe a wide range of wavelengths simultaneously, our data provides an excellent opportunity to study the correlation between different spectral features and activity indexes. Furthermore, the long duration of our observing program, the HK α Project, (~14 yr) allows us to analyze if the relation between these indexes depends on the level of activity of each individual star and, therefore, if it is associated to the distribution of active regions in the stellar atmosphere.

Díaz et al. (2007a) studied the Na I D lines (D₁: 5895.92 Å D₂: 5889.95 Å) in our stellar sample with CASLEO spectra. They constructed a spectral index (R'_D) as the ratio between the flux in the D lines and the bolometric flux. They concluded that this index, once corrected for the photospheric contribution, can be used as a chromospheric activity indicator in stars with H α in emission. Using high-resolution HARPS spectra, Gomes da Silva et al. (2011) were able to integrate the D line flux in narrower windows and, in 70% of their sample of M stars, they found a significant correlation with the Ca flux, even at low activity levels. In particular, they always obtained a positive correlation for each individual star.

In Figure 3(a) we plot simultaneous measurements of the R'_D index versus the Ca II K fluxes derived from CASLEO spectra of AD Leo. For the non-flaring points, both indexes anti-correlate with a Pearson's correlation coefficient of R = -0.63. If we remove the maximum R'_D , a possible anti-correlation is still

present, but much less significant (R = -0.39). This tendency changes during flares when both activity indicators correlate with R = 0.43.

Although in the Sun the correlation between the Ca II K and H α line-core fluxes is positive (Livingston et al. 2007), Cincunegui et al. (2007a) reported that this relation is not always valid for other late stars (F7V–M5V). Each star shows a particular behavior, ranging from anti-correlations to tight correlations with different slopes, including cases where no correlations are found (Cincunegui et al. 2007a). Based on this result, Meunier & Delfosse (2009) studied the H α –Ca II relation during the solar cycle and they found that this correlation and the slope were much larger during the solar maximum than during the minimum. In Buccino et al. (2012), we show simultaneous measurements of the H α and Ca II K+H fluxes for three solar analogs of different ages. Although they show a low correlation for the whole series, the correlation is strongly positive during active phases.

In several M stars of our sample we found that H α and the CaII K fluxes were not correlated (Díaz et al. 2007b; Buccino et al. 2011). Walkowicz & Hawley (2009) studied this correlation for several M3 dwarfs, using one spectrum for each star, and found a strong positive correlation between simultaneous measurements of CaII K and H α for the most active stars with H α in emission, including AD Leo. However, they did not analyze this relation for individual observations of each star.

Here, we compute the H α flux as the average surface flux in a 1.5 Å square passband centered in 6562.82 Å (Cincunegui et al. 2007a). In Figure 3(b) we plot the H α and CaII K fluxes for the spectra used in Figure 1(a). Both fluxes are not correlated (R = -0.145). However, as we found for solar analogs, those points associated with high activity show a rather strong correlation, with coefficient R = 0.64, and are also correlated during flares, with R = 0.65. These points are shown as triangles in Figure 3(b).

4. DISCUSSION

To explore the dynamo near the fully convective boundary, we studied the long-term activity of the M3Ve dwarf star AD Leo (GJ 388). In particular, we analyzed the Ca II K line-core fluxes measured on our CASLEO spectra obtained since 2001, and the ASAS photometric data. We obtained a possible activity cycle of approximately seven years and a less-significant shorter one of approximately two years with the Lomb-Scargle periodogram for both the photometry and in the CaII fluxes. It should be noted that we detected similar periods in two completely independent data sets. This reinforces the significance of the detection, since the probability of a false detection in both data sets should be computed as the product of both FAPs. The longer cycle falls within the statistical error of the periodic variations in the flare frequency (for energies above 10^{30} erg) reported by Pettersen et al. (1986). Furthermore, the minimum of the approximately seven year cycle reached in 2007 also coincides with a significant decrease in flare activity (Konstantinova-Antova et al. 2008).

Multiple cycles have been already detected in several cool stars (e.g., Saar & Brandenburg 1999; Oláh et al. 2009; Metcalfe et al. 2013). For those stars later than F5 with well-determined rotation and cycle periods, Saar (2011) examined the relation between the cycle (ω_{cyc}) and rotation frequencies (Ω) and found that most cycles fall into three parallel tracks, with $\omega_{cyc} \sim \Omega^{1.1}$, with double cycles falling in different branches. Therefore,

both periods are not independent. In fact, given the primary period of AD Leo of around 2800 days and its rotation period of 2.23 days, Saar's results imply that if this star presents a secondary cycle, its period should be around 800 days, similar to the one we obtained. A possible interpretation for this bimodal relation is that each activity cycle has different physical sources (Böhm-Vitense 2007). Possibly two dynamos may be operating inside the star: one driven by rotational shear in the near-surface layers (the longer cycle) and the other in the deep convection zone (the shorter cycle). Since AD Leo is a near fully convective star, unlike the stars considered in Böhm-Vitense (2007), a tachocline dynamo may not be feasible in this star.

Since we have simultaneous observations of different spectral features we can analyze the relation between chromospheric lines formed at different depths along the activity cycle and during flares. In particular, we found evidence of a possible anticorrelation between the Na I index and the Ca II K fluxes. On the other hand, the H α and Ca II fluxes show little correlation during from different magnetic structures, like spots and faculae, the resulting fluxes change during the cycle as the filling factors for each of these structures change. Therefore, the correlation between fluxes can depend on each line's contrasts (see Mauas & Falchi 1996).

In particular, during flares we find a positive correlation between the CaII, NaI, and H α fluxes, suggesting that the flare-heating mechanism in operation from the mid- to highchromosphere does not change with flare strength, as suggested by Hawley et al. (2003).

M dwarfs are ideal targets to search for terrestrial planets in the habitable zone. However, their activity signatures can hinder the detection of orbiting planets. Our results suggest that the level of activity will be appreciably lower during the next minimum, expected around 2015. This should be the best time to search for planets orbiting AD Leo.

Facility: ASAS

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