

Nuclear magnetic resonance shielding constants and chemical shifts in linear ^{199}Hg compounds: A comparison of three relativistic computational methods

Vaida Arcisauskaite, Juan I. Melo, Lars Hemmingsen, and Stephan P. A. Sauer

Citation: *The Journal of Chemical Physics* **135**, 044306 (2011); doi: 10.1063/1.3608153

View online: <https://doi.org/10.1063/1.3608153>

View Table of Contents: <http://aip.scitation.org/toc/jcp/135/4>

Published by the [American Institute of Physics](#)

Articles you may be interested in

Density functional calculations of nuclear magnetic shieldings using the zeroth-order regular approximation (ZORA) for relativistic effects: ZORA nuclear magnetic resonance

The Journal of Chemical Physics **110**, 7689 (1999); 10.1063/1.478680

Relativistic regular two-component Hamiltonians

The Journal of Chemical Physics **99**, 4597 (1993); 10.1063/1.466059

Toward reliable density functional methods without adjustable parameters: The PBE0 model

The Journal of Chemical Physics **110**, 6158 (1999); 10.1063/1.478522

Optimized basis sets for the calculation of indirect nuclear spin-spin coupling constants involving the atoms B, Al, Si, P, and Cl

The Journal of Chemical Physics **133**, 054308 (2010); 10.1063/1.3465553

A fully relativistic method for calculation of nuclear magnetic shielding tensors with a restricted magnetically balanced basis in the framework of the matrix Dirac–Kohn–Sham equation

The Journal of Chemical Physics **128**, 104101 (2008); 10.1063/1.2837472

A simple scheme for magnetic balance in four-component relativistic Kohn–Sham calculations of nuclear magnetic resonance shielding constants in a Gaussian basis

The Journal of Chemical Physics **136**, 014108 (2012); 10.1063/1.3671390

PHYSICS TODAY

WHITEPAPERS

ADVANCED LIGHT CURE ADHESIVES

Take a closer look at what these environmentally friendly adhesive systems can do

READ NOW

PRESENTED BY
 **MASTERBOND**
ADHESIVES | SEALANTS | COATINGS

Nuclear magnetic resonance shielding constants and chemical shifts in linear ^{199}Hg compounds: A comparison of three relativistic computational methods

Vaida Arcisauskaitė,^{1,a)} Juan I. Melo,² Lars Hemmingsen,¹ and Stephan P. A. Sauer³

¹*Department of Basic Sciences and Environment, Faculty of LIFE Sciences, University of Copenhagen, Thorvaldsensvej 40, DK-1871 Frederiksberg, Denmark*

²*Departamento de Física, Facultad de Ciencias Exactas y Naturales, Universidad de Buenos Aires, Ciudad Universitaria, Pab. 1, 1428 Buenos Aires, Argentina and CONICET*

³*Department of Chemistry, University of Copenhagen, Universitetsparken 5, DK-2100 Copenhagen Ø, Denmark*

(Received 16 June 2010; accepted 16 June 2011; published online 26 July 2011)

We investigate the importance of relativistic effects on NMR shielding constants and chemical shifts of linear HgL_2 ($L = \text{Cl}, \text{Br}, \text{I}, \text{CH}_3$) compounds using three different relativistic methods: the fully relativistic four-component approach and the two-component approximations, linear response elimination of small component (LR-ESC) and zeroth-order regular approximation (ZORA). LR-ESC reproduces successfully the four-component results for the C shielding constant in $\text{Hg}(\text{CH}_3)_2$ within 6 ppm, but fails to reproduce the Hg shielding constants and chemical shifts. The latter is mainly due to an underestimation of the change in spin-orbit contribution. Even though ZORA underestimates the absolute Hg NMR shielding constants by ~ 2100 ppm, the differences between Hg chemical shift values obtained using ZORA and the four-component approach without spin-density contribution to the exchange-correlation (XC) kernel are less than 60 ppm for all compounds using three different functionals, BP86, B3LYP, and PBE0. However, larger deviations (up to 366 ppm) occur for Hg chemical shifts in HgBr_2 and HgI_2 when ZORA results are compared with four-component calculations with non-collinear spin-density contribution to the XC kernel. For the ZORA calculations it is necessary to use large basis sets (QZ4P) and the TZ2P basis set may give errors of ~ 500 ppm for the Hg chemical shifts, despite deceptively good agreement with experimental data. A Gaussian nucleus model for the Coulomb potential reduces the Hg shielding constants by ~ 100 – 500 ppm and the Hg chemical shifts by 1–143 ppm compared to the point nucleus model depending on the atomic number Z of the coordinating atom and the level of theory. The effect on the shielding constants of the lighter nuclei (C, Cl, Br, I) is, however, negligible. © 2011 American Institute of Physics. [doi:10.1063/1.3608153]

I. INTRODUCTION

The coordination chemistry of Hg(II) is important in its own right, and, in particular, because mercury ions may substitute native metal ions in metalloproteins, probably giving rise to the well known toxic effects of this heavy metal ion. ^{199}Hg NMR spectroscopy has become a powerful tool in this context due to the sensitivity of the ^{199}Hg NMR shielding constants and chemical shifts to the first coordination sphere of Hg(II).^{1–3}

Relativistic effects play an important role for NMR properties of systems containing heavy elements, such as mercury. From a computational point of view, there are several ways of treating relativistic effects. The first option is fully relativistic four-component linear response calculations⁴ within program packages, such as DIRAC,^{4–8} BERTHA,⁹ MOLFDIR,¹⁰ BDF,¹¹ and ReSpect.^{12,13} A second option is computationally less demanding two-component methods, such as the zeroth-order regular approximation (ZORA),^{14–18} exact two-component

methods,^{19,20} Douglas-Kroll-Hess (DKH) approaches,^{21–25} or the perturbational schemes by Melo *et al.*,^{26,27} by Vaara *et al.*,^{7,28,29} and the direct perturbation theory approach by Kutzelnigg.³⁰

The first *ab initio* calculations including relativistic effects of ^{199}Hg NMR shielding constants in mercury halides were presented by Nakatsuji *et al.*³¹ They used a method which is a combination of a relativistic spin-free no-pair theory and the spin-orbit (SO) unrestricted Hartree-Fock (HF) method and concluded that spin-free terms, such as the mass-velocity and Darwin terms, and the spin-orbit term are important and that they strongly couple with each other. Moreover, they showed that for ^{199}Hg NMR shielding constants and chemical shifts the spin-orbit term of the halogen becomes more important for the heavier halogens. This conclusion was also supported by the study of Fukuda *et al.*²⁴ who employed a method based on the DKH transformation. They also state that for more accurate predictions of the chemical shifts of these molecules one should consider electron correlation effects. Using ZORA at the density functional theory (DFT) level, Wolff *et al.*¹⁸ showed that mercury NMR shielding

^{a)}Electronic mail: vaida@life.ku.dk.

constants strongly depend on the structure of mercury halides. Finally, Taylor *et al.*³² conducted recently a ZORA-DFT study on ¹⁹⁹Hg NMR shielding constants of Hg(CH₃)₂, solid HgCl₂, and of HgCl₂ complexed with DMSO. To the best of our knowledge, four-component relativistic calculations of NMR shielding constants have not yet been presented for Hg(II) compounds, except that Fukuda *et al.*²³ employed the four-component/Dirac-Hartree-Fock (DHF) (Ref. 33) approach to calculate the ¹⁹⁹Hg NMR shielding constant for Hg⁷⁸⁺ and Hg⁷⁰⁺ ions and Seino and Hada²⁵ employed a four-component scheme to calculate the NMR shielding constant of the Hg atom. On the other hand, four-component relativistic calculations of NMR shielding constants were performed for several other heavy metal compounds. Lantto *et al.*⁷ have carried out DHF calculations on X²⁺, X⁴⁺, XH₂, and XH₃⁻ (X = Si–Pb) as well as X³⁺, XH₃, and XF₃ (X = P–Bi) systems and very recently Melo *et al.*³⁴ carried out DHF calculations on SnH₂XY and PbH₂XY (XY = F, Cl, Br, and I).

The goal of this study is thus (1) to compare the results of the approximate, two-component relativistic methods, linear response elimination of small component (LR-ESC) and ZORA, with results of fully relativistic four-component calculations of shielding constants and chemical shifts for linear-coordinated Hg(II) containing molecules, (2) to test convergence of the calculated shielding constants with basis set size, (3) to study the effect of using a Gaussian charge distribution model for the nuclear Coulomb potential as opposed to a point charge model, (4) to compare HF and DFT methods with different functionals, and finally (5) to compare the calculated Hg chemical shifts with experimental data. For that purpose we compare the performance of the three different relativistic methods (fully relativistic four-component calculations with the DIRAC program,^{35,36} LR-ESC calculations with the DALTON code,³⁷ and ZORA calculations as implemented in the ADF program³⁸) for the NMR shielding constants of all nuclei and the Hg chemical shifts in linear HgL₂ (L = Cl, Br, I, CH₃) compounds. Moreover, we investigate how much the choice of the common gauge origin (GO) and non-collinear spin-density contribution to the exchange-correlation (XC) kernel influence the outcome of the calculations.

II. COMPUTATIONAL DETAILS

A. Four-component calculations

Four-component fully relativistic shielding constant calculations with a common gauge origin for the vector potential were carried out using the DIRAC v.08 code³⁵ at the DHF and DFT levels. DIRAC v.10 version³⁶ was released during the revision of the paper and was employed for calculations using gauge-including atomic orbitals (GIAO) (Refs. 8 and 39) as well as for calculations with non-collinear spin density contribution to the XC kernel (non-collinear spin-magnetization). In addition to the hybrid B3LYP (Refs. 40 and 41) and PBE0 (Refs. 42–45) functionals, we employed the generalised gradient approximation (GGA) BP86 (Refs. 46 and 47) functional, which has been used previously in calculations of ¹⁹⁹Hg NMR shielding constants in Ref. 32 and 48. The nuclear magnetic shielding constant was calculated as four-component linear response functions.⁴ In order to re-

duce the computational cost, we performed approximate Dirac-Coulomb calculations, where the interatomic small component–small component (SS) integral contribution is modelled by the classical repulsion of small component atomic charges as proposed by Visscher.⁴⁹ In addition, we used the unrestricted kinetic balance (UKB) condition,⁵⁰ which in contrast to the restricted kinetic balance (RKB) condition⁵⁰ allows to modify the coupling towards the magnetic balance between the large and small components of the relativistic wave function. It was shown that UKB ensures convergence of nuclear magnetic shielding constants with smaller basis sets than using the RKB condition.^{8,51–54} In order to properly describe NMR shielding constants we use basis sets which contain tight functions. For the Hg, Br, and I atoms we used the basis sets by Dyall^{55,56} dyall.cvxx (x=2,3,4) and for Cl, C, and H – Dunning’s cc-pCVXZ (X=D,T,Q) basis sets were used,^{57,58} all in their completely uncontracted form. The threshold value for convergence in the error vector (electronic gradient) was set to 1.0D-7. The convergence of the shielding constants with the basis set is discussed in Sec. III.

Three other computational issues have been addressed. The first issue refers to the choice of gauge origin of the vector potential within the common gauge origin approach and to the comparison with GIAO results at the DHF level (using DIRAC v.10) and is discussed in Sec. III. In the common GO case, the gauge origin was placed at the heavy nucleus Hg when calculating ¹⁹⁹Hg NMR shielding constants, whereas in calculations of NMR shielding constants of lighter nuclei (Cl, Br, I, C, H), the gauge origin was placed either at the position of the nucleus in question or at the Hg nucleus. The second issue concerns the choice of the nuclear charge model for the Coulomb potential of the nuclei. Here, we have used both a Gaussian charge distribution or a point charge model for the Coulomb potential, whereas in the expression for the vector potential of the nuclear magnetic moment, only a point nucleus model is available. Consequently, we introduce the following abbreviations, which are used throughout the paper. *p.p.* or point/point indicates that the point nucleus model has been used for both the Coulomb and vector potential of the nucleus, while *g.p.* or Gaussian/point implies that a Gaussian charge distribution was used for the Coulomb and a point nucleus model for the vector potential of the nuclear magnetic moment. The Gaussian charge distribution nuclear model is a more physical model to describe the nuclear charge distribution than the point charge model and we employ a Gaussian charge distribution with exponents proposed by Visscher and Dyall.⁵⁹ The results of this study are presented in Sec. IV. The last issue investigates how non-collinear spin-density contribution to the XC kernel changes the shielding constant and Hg chemical shift values in DFT calculations and is discussed in Sec. V.

B. LR-ESC calculations

LR-ESC calculations were carried out using the DALTON v2.0 code³⁷ at HF and DFT/BP86 levels with the exception of the σ (DIA-K) contributions,⁶⁰ which are implemented in a local development version of DALTON v2.0. In

the LR-ESC scheme, the total relativistic nuclear magnetic shielding constant is calculated as the sum of the non-relativistic (NR) shielding constants and corrections according to the Rayleigh-Schrödinger perturbation theory expressions.^{26,27} Dyall's dyall.cvxx ($x=2,3,4$) basis sets were used for Hg, Br, I, whereas H, C, and Cl were described using Dunning's cc-pCVXZ ($X=D,T,Q$) basis sets, all in their uncontracted form. Employed basis sets had enough tight functions in order to obtain converged paramagnetic LR-ESC terms.^{27,60} A convergence threshold of $1.0D-06$ for the energy gradient was used. The basis set convergence is discussed in Sec. III. Although it was previously shown that the LR-ESC scheme is gauge invariant in the limit of a complete basis set (CBS),⁶¹ in actual calculations using a finite basis set gauge origin independence can only be achieved by special methods such as the distributed gauge origin methods GIAO, individual gauge for localized orbitals (IGLO),^{62,63} or continuous transformation of the origin of the current density (CTOCD).⁶⁴⁻⁶⁶ As none of these have been implemented for the relativistic corrections in the LR-ESC approach, we have used GIAOs in the calculation of the non-relativistic shielding constants⁶⁷ and the common-origin approach with the gauge origin fixed at the position of each studied nucleus or other nucleus for the relativistic corrections in the LR-ESC approach which is more thoroughly discussed in Sec. III. Concerning the choice of nuclear charge model for the Coulomb potential of the nuclei in the LR-ESC scheme, which combines a non-relativistic shielding constant calculation with relativistic corrections to it, it is more consistent to use only the point nucleus model (*p.p.*) in both the non-relativistic and relativistic calculations. For the vector potential of the nuclear magnetic moment only the point nucleus model is available. Spin-density contribution in the LR-ESC-DFT scheme appears in the property calculation part through coupling of spin-dependent perturbation operators with perturbed states which may not have a zero spin.

C. ZORA calculations

NMR shielding constants were also calculated with the ZORA approach.¹⁴⁻¹⁷ All calculations were carried out using the NMR module^{18,68,69} of the ADF v.2009.01 program³⁸ at the DFT level with the BP86, B3LYP, and PBE0 functionals. ZORA relativistic Slater type all-electron basis sets⁷⁰ were used in the form of GIAOs.⁷¹⁻⁷³ As recommended by ADF developers, for accurate hybrid calculations we added more diffuse fit functions and used the strict criteria for the basis set dependence, namely, $bas = 1 \times 10^{-4}$. The threshold value for convergence in the error vector was set to $1.0D-8$. In the ZORA calculations, as in the four-component calculations, we could choose between the Gaussian charge distribution and the point charge model for the Coulomb potential, but we had only the option of a point nucleus model for the vector potential of the nuclear magnetic moment. Thus, we performed *g.p.* and *p.p.* calculations.

Spin-orbit coupling is included variationally in the solution of the Kohn-Sham equations for the closed shell ground state. In the solution of the DFT response equations, necessary for the calculation of the shielding constants, the ex-

TABLE I. Experimental gas phase electron diffraction geometries of HgL_2 ($L = Cl, Br, I, CH_3$) compounds used in this study. Bond lengths are in Å and angles are in degrees.

Molecule	Geometry
$HgCl_2$	$r(Hg-Cl) = 2.252 \pm 0.005^a$
$HgBr_2$	$r(Hg-Br) = 2.41 \pm 0.01^b$
HgI_2	$r(Hg-I) = 2.554 \pm 0.003^c$
$Hg(CH_3)_2$	$r(Hg-C) = 2.083 \pm 0.003^d$ $r(C-H) = 1.106$ (assumed) ^d $\angle(H-C-H) = 109.5$ (assumed)

^aGeometry taken from Ref. 74.

^bGeometry taken from Ref. 75.

^cGeometry taken from Ref. 76.

^dGeometry taken from Ref. 77.

ternal magnetic field perturbation leads to a first order spin-density and, consequently, to a Fermi-contact (-like) contribution to the NMR shielding constant, which is calculated in the ADF NMR calculation. However, the contribution to the DFT part of the exchange-correlation kernel of the response equations is neglected in ADF contrary to the four-component calculations with spin-density contribution to the XC kernel. Therefore, only uncoupled perturbed Kohn-Sham equations are solved for GGA or local-density approximation functionals in the ADF NMR calculations. In the case of hybrid functionals, such as B3LYP, the Hartree-Fock exchange potential leads furthermore to a first order change of the orbitals due to the external magnetic field, which makes it necessary to solve coupled perturbed Kohn-Sham equations, but the first order spin-density is still not taken into account in the DFT part of the exchange-correlation potential.^{68,69}

D. Geometries of Hg compounds

NMR shielding constants were calculated for linear HgL_2 ($L = Cl, Br, I, CH_3$) compounds. We used experimental geometries (see Table I for details) obtained with electron diffraction in the gas phase.⁷⁴⁻⁷⁷ For $Hg(CH_3)_2$ nearly free rotation of the methyl groups was reported;⁷⁷ therefore, the $Hg-CH_3$ bond-length (2.083 Å) was interpreted as the average configuration. We chose to test two different positions of methyl groups—with dihedral angle 0° in eclipsed structure and dihedral angle 60° in staggered structure, using ADF/ZORA approach. We obtained Hg NMR shielding constants: $\sigma(^{199}Hg) = 7929$ ppm and $\sigma(^{199}Hg) = 7932$ ppm for the eclipsed and staggered structures, respectively. Herein, we used the BP86 functional, the point/point nucleus models, and a TZ2P basis set. We conclude, that both conformations give virtually identical Hg shielding constants and both results are in a good agreement with the earlier result $\sigma(^{199}Hg) = 7929$ ppm obtained by Taylor *et al.*³² using ADF/ZORA with the same functional and basis set. In the following we will therefore only consider the eclipsed conformer.

III. SELECTION OF BASIS SET AND GAUGE ORIGIN

We have investigated the basis set dependence of the shielding constants calculated with all three relativistic methods for the smallest halogen system $HgCl_2$. The

TABLE II. **Basis set dependence of four-component calculations:** shielding constants, $\sigma(^{199}\text{Hg})$ and $\sigma(^{35}\text{Cl})$, (in ppm) of HgCl_2 as a function of different basis sets calculated using the four-component method at the Dirac-Hartree-Fock (DHF) and DFT/BP86 levels in combination with Gaussian/point nucleus models.

Basis set Hg/Cl	$\sigma(^{199}\text{Hg})$			$\sigma(^{35}\text{Cl})$			
	GIAO	GO=Hg		GIAO	GO=Hg		GO=Cl
	DHF	DHF	DFT	DHF	DHF	DFT	DHF
dyall.cv2z/cc-pCVDZ	13 600	13 732	12 203	1124	1194	894	884
dyall.cv3z/cc-pCVTZ	13 580	13 605	12 049	1126	1145	860	918
dyall.cv4z/cc-pCVQZ	13 613	13 618	12 049	1131	1137	856	947

four-component, LR-ESC, and ZORA results are presented in Tables II, III, and V, respectively.

In the four-component and LR-ESC calculations we have employed Dyall's^{55,56} basis sets dyall.cv2z (22s19p12d9f1g), dyall.cv3z (29s24p15d11f4g1h), and dyall.cv4z (34s30p19d13f4g2h) for Hg and Dunning's^{57,58} basis sets cc-pCVDZ (13s9p2d), cc-pCVTZ (17s11p4d2f), and cc-pCVQZ (19s14p6d4f2g) for Cl. Both series of basis sets are designed to converge systematically to the CBS limit of the total energy. Dunning's correlation consistent basis set has frequently also been used in extrapolation schemes for NMR shielding and spin-spin coupling constants.^{78,79}

In Table II we present results of the basis set study for four-component calculations. The DHF gauge independent (GIAO) calculations give similar values of the NMR shielding constant, $\sigma(^{199}\text{Hg})$, with all three basis sets, and thus appear to be converged to within 20 ppm already with the dyall.cv2z/cc-pCVDZ basis set. With the gauge origin placed at Hg the shielding constant changes only marginally between the two largest basis sets and thus also appears to be converged. This is further supported by the fact that the results converge towards those obtained with the GIAO method, displaying a difference of 132 ppm, 25 ppm, and 5 ppm with the dyall.cv2z/cc-pCVDZ, dyall.cv3z/cc-pCVTZ, and dyall.cv4z/cc-pCVQZ basis sets, respectively. Finally, at the DFT/BP86 level the dyall.cv3z/cc-pCVTZ and dyall.cv4z/cc-pCVQZ basis sets give the same Hg shielding constant value of 12 049 ppm, indicating that the dyall.cv3z/cc-pCVTZ basis set is already close to the CBS limit. Regarding the Cl NMR shielding constant, the trends are similar for the GIAO calculations and when the gauge origin is placed at Hg. However,

TABLE III. **Basis set dependence of LR-ESC calculations:** shielding constants, $\sigma(^{199}\text{Hg})$ and $\sigma(^{35}\text{Cl})$, (in ppm) of HgCl_2 as a function of different basis sets calculated using the LR-ESC method at the HF level in combination with point/point nucleus models. The total relativistic nuclear magnetic shielding constant is calculated as the sum of non-relativistic shielding constants (obtained by GIAO) and corrections according to the Rayleigh-Schrödinger perturbation theory expressions (obtained by common gauge origin (GO)).

Basis set	$\sigma(^{199}\text{Hg})$	$\sigma(^{35}\text{Cl})$
	GO=Hg	GO=Cl
dyall.cv2z/cc-pCVDZ	10 487	1054
dyall.cv3z/cc-pCVTZ	10 514	1173
dyall.cv4z/cc-pCVQZ	10 664	1179

placing the gauge origin at Cl gives a significantly different shielding constant and poorer convergence. Consequently, in the following DHF and DFT calculations, we place the GO at Hg, and in order to save computational resources, we decided to use the dyall.cv3z basis set for Hg, Br, I and the cc-pCVTZ basis set for H, C, Cl in all further four-component calculations.

The results of a basis set study for the LR-ESC approach at the HF level are presented in Table III. We do not observe as good convergence for the Hg shielding constant as in the four-component calculations. The difference between the Hg shielding constant values obtained using dyall.cv3z/cc-pCVTZ and dyall.cv4z/cc-pCVQZ is about 5 times larger than going from dyall.cv2z/cc-pCVDZ to dyall.cv3z/cc-pCVTZ. Thus, this is a slight divergence of the LR-ESC results with increasing the basis set. The dyall.cv3z result for the Hg NMR shielding constant differs by 1.5% (150 ppm) from the dyall.cv4z/cc-pCVQZ result. For Cl, on the other hand, the difference amounts to only 0.5% (6 ppm). To put the remaining basis set errors into perspective, it is useful to compare this with the deviations from the four-component results with the same basis set, which amount to 23% (3091 ppm) for Hg and 2.5% (29 ppm) for Cl using the dyall.cv3z/cc-pCVTZ basis set. We consider thus that the remaining basis set error in the LR-ESC results for Hg is irrelevant compared to the one order of magnitude larger deviations

TABLE IV. **The choice of gauge origin (GO) in LR-ESC:** shielding constants, $\sigma(N)$ ($N = \text{Hg}, \text{C}, \text{Cl}, \text{Br}, \text{I}$), were calculated as the sum of non-relativistic shielding constants (obtained by GIAO) and LR-ESC corrections at the HF level in combination with point/point nucleus models and dyall.cv3z basis set for Hg, Br, I and cc-pCVTZ basis set for H, C, Cl. We calculated LR-ESC corrections using the common-origin approach with the GO fixed either at the position of each studied nucleus N or fixed at the position of the other nucleus.

Molecule	N	NR	LR-ESC corrections		LR-ESC total	
		GIAO	GO= N	GO=other	GO= N	GO=other
$\text{Hg}(\text{CH}_3)_2$	Hg	6695.0	2755.7	2755.2	9450.7	9450.2
HgCl_2	Hg	7548.4	2965.6	2965.6	10 514.0	10 514.0
HgBr_2	Hg	7541.4	3100.0	3100.1	10 641.4	10 641.5
HgI_2	Hg	7177.1	3280.6	3280.8	10 457.7	10 457.9
$\text{Hg}(\text{CH}_3)_2$	C	217.8	-42.6	-35.9	175.2	181.9
HgCl_2	Cl	1201.7	-28.5	-27.3	1173.2	1174.4
HgBr_2	Br	3162.9	124.0	121.5	3286.9	3284.4
HgI_2	I	5455.8	735.6	733.4	6191.4	6189.2

TABLE V. **Basis set dependence of ZORA calculations:** shielding constants, $\sigma(^{199}\text{Hg})$ and $\sigma(^{35}\text{Cl})$, (in ppm) of HgCl_2 as a function of different basis sets calculated using the ZORA method at the DFT/BP86 level in combination with Gaussian/point nucleus models.

Basis set	$\sigma(^{199}\text{Hg})$	$\sigma(^{35}\text{Cl})$
	GIAO	GIAO
DZ	9732	817
TZ	10 452	874
TZP	9606	853
TZ2P	9541	854
QZ	10 408	862
QZ2P	9957	837
QZ4P	9948	835

from the four-component results and that it has no significant impact on our conclusions concerning the performance of the LR-ESC method for the Hg shielding constants presented in this work. As we prefer to use in the LR-ESC calculations a basis set as similar to one of the four-component calculations as possible and because four-component calculations for the heavier systems using the dyall.cv4z/cc-pCVQZ basis set are too resource demanding, we will in all further LR-ESC calculations employ the dyall.cv3z for Hg, Br, I and cc-pCVTZ for H, C, Cl. We have also investigated the effect of moving the common gauge origin in the calculation of the relativistic corrections from the nucleus of interest to the other nucleus. The results of this study are presented in Table IV. LR-ESC corrections to the Hg shielding constant change by at most 0.5 ppm due to the change of gauge origin, whereas at most 2.5 ppm and 6.7 ppm differences are observed for halogen and C shielding constants, respectively. This confirms the results of a very recent study on the shielding constants in SnH_2F_2 ,³⁴ where a similarly small gauge origin dependence of LR-ESC results was observed. Due to the small gauge origin dependence of LR-ESC results, in the following calculations we place the gauge origin at the nucleus of interest only.

The results of the basis set study with the ZORA approach are given in Table V. We have used all the ZORA relativistic Slater type all-electron basis sets, which are provided by the ADF program for Hg and Cl: DZ ($13s10p6d3f/6s4p$), TZP ($14s10p7d3f/7s5p1d$), TZ2P ($14s10p7d4f/7s5p1d1f$), QZ4P ($22s18p12d6f/11s7p3d2f$) for Hg/Cl, respectively. In order to perform a thorough basis set convergence study, we additionally constructed TZ ($14s9p7d3f/7s5p$), QZ ($22s15p11d4f/11s7p$), and QZ2P ($22s17p12d5f/11s7p2d1f$) basis sets, by eliminating polarisation functions or replacing polarisation functions from the TZP and QZ4P basis sets with smaller number of functions with the average exponent (these basis sets are available as supplementary material⁸⁰). Here, there appear to be two opposing basis set convergence patterns. First, in the $\text{DZ} \Rightarrow \text{TZ} \Rightarrow \text{QZ}$ series the shielding constant varies as 9732 ppm \Rightarrow 10 452 ppm \Rightarrow 10 408 ppm. Thus, the TZ result differs by less than 50 ppm from the QZ result and there seems to be convergence to within this error in this series. When polarisation functions are added to the TZ and QZ basis sets, the Hg NMR shielding constant decreases (the same is observed for Cl NMR shielding constant) and appears to be converged to within 10 ppm in the series QZ

$\Rightarrow \text{QZ2P} \Rightarrow \text{QZ4P}$. One could expect that adding more polarisation functions to the TZ2P basis set would lead to further reduction. But it is not possible to verify this within this work due to technical difficulties arising when adding polarisation functions. As a consequence of the opposing trends the standard ADF basis sets, TZ2P and QZ4P, give quite different Hg NMR shielding constant results (9541 ppm and 9948 ppm, respectively). For Cl the trends are quite similar to those observed for Hg, although TZ2P and QZ4P give results which are closer (854 ppm and 835 ppm, respectively). In the following we will employ the largest possible basis set, QZ4P, which also contains the largest number of high-exponent functions, important for the calculation of shielding constants and especially the spin-orbit term.

IV. SELECTION OF THE NUCLEAR CHARGE MODEL FOR THE COULOMB POTENTIAL

In this section the selection of the nuclear charge model for the Coulomb potential in four-component and ZORA calculations is described. A Gaussian charge distribution or a point charge model for the Coulomb potential are applied together with a point nucleus model for the vector potential of the nuclear magnetic moment using the nomenclature Gaussian/point (*g.p.*) and point/point (*p.p.*) in the tables. The outcome of this investigation at the level of DFT/BP86 is presented in Table VI. From this we deduce that using a finite nucleus for the Coulomb potential reduces the Hg shielding constants by ~ 100 – 500 ppm (about 1%–3%). A similar study was conducted by Fukuda *et al.*²³ who compared the values of heavy ion (including Hg^{70+} and Hg^{78+}) shielding constants obtained by point and Gaussian nucleus models for both the Coulomb and vector potential of the nuclear magnetic moment using DHF and a two-component quasirelativistic theory based on the DKH transformation. Their conclusion was that using a Gaussian nucleus model gives rise to a decrease of the Hg shielding constant values by ~ 500 ppm compared to calculations using a point nucleus model for Hg^{70+} and Hg^{78+} ions. Interestingly, the chemical shift, $\delta(^{199}\text{Hg})$, is also affected by the choice of nuclear model. In the four-component calculations the change from a point nucleus to a Gaussian nucleus model is 10 ppm, 70 ppm, and 143 ppm for HgCl_2 , HgBr_2 , and HgI_2 , respectively. That is, it depends on the atomic number Z of the coordinating atom. For the ZORA calculations the same series gives a difference of 1 ppm, 40 ppm, and 97 ppm, and thus recovers from 10% to 68% of the finite nucleus effect observed with the four-component method. It is noteworthy that the observed reductions in ZORA calculations can be linked to the changes in the spin-orbit term (data not shown), and this is in a good agreement with the statement that the finite nucleus model affects the hyperfine structures of heavy atoms.^{81,82}

For the shielding constants of the lighter atoms the effect is negligible (~ 0 – 1 ppm) and for iodine the change of the shielding constant is 15 ppm using the four-component method.

In Sec. V, we will present four-component and ZORA results which are obtained using the Gaussian nucleus model for the Coulomb potential.

TABLE VI. **Nuclear charge model:** shielding constants, $\sigma(N)$ ($N = \text{Hg, C, Cl, Br, I}$), and chemical shifts, $\delta(^{199}\text{Hg})$, of HgL_2 ($L = \text{CH}_3, \text{Cl, Br, I}$) compounds (in ppm) calculated using four-component and ZORA approaches in combination with DFT/BP86, point/point (*p.p.*), and Gaussian/point (*g.p.*) nuclear models for the Coulomb and vector potentials, respectively. The Hg chemical shift is calculated as $\delta(^{199}\text{Hg}_{\text{HgL}_2}) = (\sigma(^{199}\text{Hg}_{\text{Hg}(\text{CH}_3)_2}) - \sigma(^{199}\text{Hg}_{\text{HgL}_2})) / (1 - \sigma(^{199}\text{Hg}_{\text{Hg}(\text{CH}_3)_2}))$.

Molecule	N	$\sigma(N)$				$\delta(^{199}\text{Hg})$			
		ZORA		Four-component		ZORA		Four-component	
		<i>p.p.</i>	<i>g.p.</i>	<i>p.p.</i>	<i>g.p.</i>	<i>p.p.</i>	<i>g.p.</i>	<i>p.p.</i>	<i>g.p.</i>
$\text{Hg}(\text{CH}_3)_2$	Hg	8084	7967	10 299	10 015				
HgCl_2	Hg	10 063	9948	12 343	12 049	−1995	−1996	−2065	−2055
HgBr_2	Hg	11 335	11 179	13 606	13 254	−3277	−3237	−3341	−3271
HgI_2	Hg	12 397	12 185	14 689	14 265	−4348	−4251	−4435	−4292
$\text{Hg}(\text{CH}_3)_2$	C	155	155	155	155				
HgCl_2	Cl	834	835	860	860				
HgBr_2	Br	2379	2381	2515	2516				
HgI_2	I	4694	4698	5212	5197				

V. RESULTS AND DISCUSSION

A. Relativistic corrections to shielding constants and Hg chemical shifts

In this section, we compare the performance of three relativistic methods (four-component, LR-ESC, and ZORA) in calculations of NMR parameters of HgL_2 ($L = \text{CH}_3, \text{Cl, Br, I}$) compounds, and describe the magnitude of the relativistic correction (i.e., the difference of the shielding constant calculated with non-relativistic and relativistic methods). The calculations were performed at the level of HF and DFT theories. Regarding the latter, we employed three different functionals (GGA/BP86 and the hybrid functionals B3LYP and PBE0). In the upper part of Table VII, shielding constants, $\sigma(N)$ ($N = \text{Hg, C, Cl, Br, I}$), are presented, whereas the bottom part of the table is dedicated to Hg chemical shifts, $\delta(^{199}\text{Hg})$.

The results of the DFT/BP86 calculations in Table VII illustrate that the relativistic corrections follow a systematic trend as a function of the atomic number of the nucleus in question. The differences between the four-component and non-relativistic results for the shielding constants of the ligand atoms increase from carbon (−41 ppm) over chlorine (−183 ppm) and bromine (−272 ppm) to iodine (+310 ppm). For carbon and probably chlorine this is due to the HALA effect (heavy atom effect on the shielding of a light atom) from the neighbouring Hg atom, whereas for bromine and iodine there are in addition HAVA effects⁸³ (heavy atom effects on the shielding of the heavy atom itself). At the same time also the relativistic correction to the Hg shielding constant increases with the atomic number of the ligand atom: 3893 ppm in $\text{Hg}(\text{CH}_3)_2$, 4846 ppm in HgCl_2 , and finally 7474 ppm in HgI_2 as shown in Fig. 1(a) and can be attributed to HAVHA effect (heavy atom effect on vicinal heavy

TABLE VII. **Comparison of relativistic methods:** shielding constants, $\sigma(N)$ ($N = \text{Hg, C, Cl, Br, I}$), and chemicals shifts, $\delta(^{199}\text{Hg})$, calculated using non-relativistic method (NR) (with GIAO) and three different relativistic methods: LR-ESC and four-component (without and with spin-density contribution to the XC kernel) using common gauge origin and ZORA using GIAO. The calculations were performed at the level of HF and DFT in combination with three different functionals BP86, B3LYP, and PBE0. The Hg chemical is calculated as $\delta(^{199}\text{Hg}_{\text{HgL}_2}) = (\sigma(^{199}\text{Hg}_{\text{Hg}(\text{CH}_3)_2}) - \sigma(^{199}\text{Hg}_{\text{HgL}_2})) / (1 - \sigma(^{199}\text{Hg}_{\text{Hg}(\text{CH}_3)_2}))$.

Molecule	N	DFT										
		HF		BP86				B3LYP		PBE0		
		NR	LR-ESC	Four-component	NR	LR-ESC	ZORA	Four-component (spin-density)	ZORA	Four-component	ZORA	Four-component
Shielding constants, $\sigma(N)$ ($N = \text{Hg, C, Cl, Br, I}$)												
$\text{Hg}(\text{CH}_3)_2$	Hg	6695	9451	12 054	6122	8533	7967	10 015 (10 276)	8326	10 381	8484	10 536
HgCl_2	Hg	7548	10 514	13 605	7203	10 010	9948	12 049 (12 306)	10 256	12 353	10 354	12 443
HgBr_2	Hg	7541	10 641	14 636	7195	10 355	11 179	13 254 (13 691)	11 450	13 528	11 454	13 526
HgI_2	Hg	7177	10 458	15 686	6791	10 403	12 185	14 265 (14 845)	12 473	14 561	12 407	14 496
$\text{Hg}(\text{CH}_3)_2$	C	218	175	169	196	156	155	155 (150)	156	156	164	164
HgCl_2	Cl	1202	1173	1145	1043	938	835	860 (860)	906	929	938	965
HgBr_2	Br	3163	3287	3246	2788	2728	2381	2516 (2539)	2549	2686	2651	2789
HgI_2	I	5456	6191	6367	4887	5369	4698	5197 (5280)	4959	5464	5133	5637
Chemical shifts, $\delta(^{199}\text{Hg})$												
HgCl_2	Hg	−859	−1073	−1570	−1087	−1489	−1996	−2055 (−2051)	−1946	−1992	−1886	−1927
HgBr_2	Hg	−851	−1201	−2613	−1079	−1838	−3237	−3271 (−3450)	−3150	−3180	−2995	−3021
HgI_2	Hg	−485	−1017	−3676	−673	−1886	−4251	−4292 (−4617)	−4181	−4223	−3956	−4002

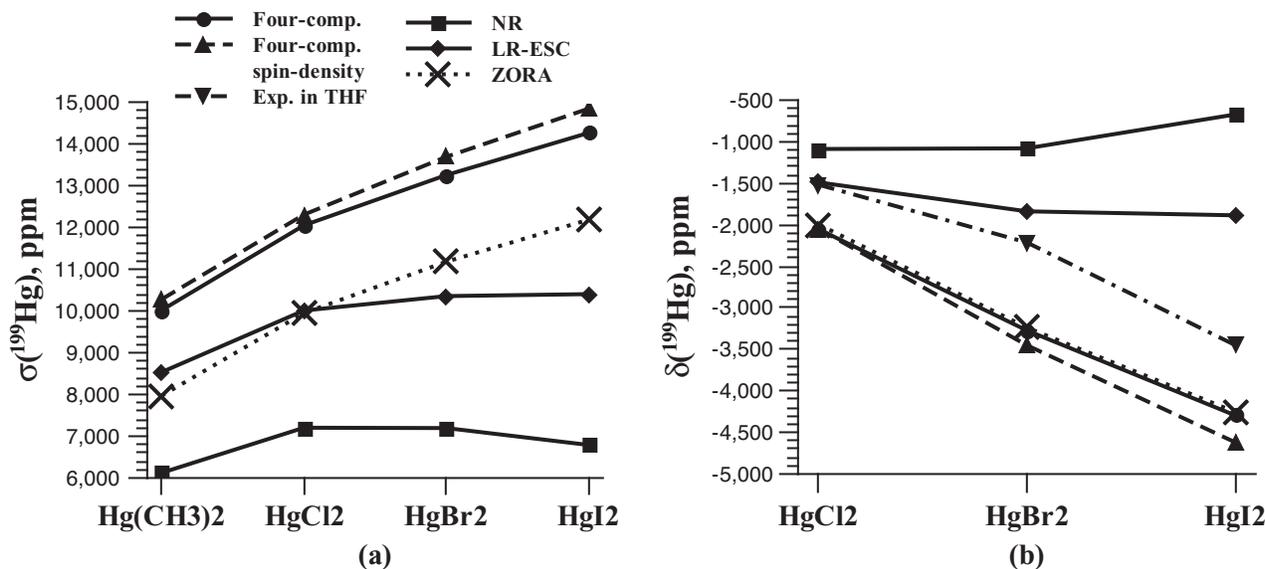


FIG. 1. (a) Shielding constants, $\sigma(^{199}\text{Hg})$, and (b) chemical shifts, $\delta(^{199}\text{Hg})$, of HgL_2 ($L = \text{CH}_3, \text{Cl}, \text{Br}, \text{I}$) compounds calculated using NR, LR-ESC, ZORA, and four-component methods at the DFT/BP86 level and determined experimentally in THF. All the calculated values are from Table VII and experimental values are from Table X.

atom).^{34,54} These trends are repeated in the HF calculations; however, the relativistic effects are somewhat larger for mercury, such as 5359 ppm in $\text{Hg}(\text{CH}_3)_2$, 6057 ppm in HgCl_2 , and finally 7095 ppm in HgI_2 , whereas the shielding constant of the ligand atoms increases in absolute value from carbon (-49 ppm) over chlorine (-57 ppm) and bromine ($+89$ ppm) to iodine ($+911$ ppm). The relativistic corrections to the mercury chemical shifts are 968 ppm, 2192 ppm, and 3619 ppm for HgCl_2 , HgBr_2 , and HgI_2 , respectively, at the level of DFT/BP86. This follows the normal halogen dependence^{84,85} behaviour in which an increased spin-orbit contribution is found for the heavier halogen ligands.^{18,24,31}

In the following paragraph the performance of the two-component methods is discussed (see also Fig. 1). For the C shielding constant, both LR-ESC and ZORA reproduce the relativistic corrections of four-component calculations. For Cl and Br, LR-ESC and ZORA behave differently; LR-ESC underestimates relativistic corrections, whereas ZORA overestimates the relativistic corrections to the shielding constants. While for I (which is also considered as heavy atom besides Hg), LR-ESC overestimates relativistic corrections and ZORA calculations even give the incorrect sign of the relativistic correction. It has previously been reported that ZORA might give errors for heavy atom properties that depend on the core orbitals, such as absolute shielding constants, whereas chemical shifts are reproduced well, *vide infra*.⁸⁶ For Hg shielding constants, LR-ESC predicts relativistic corrections of 2411 ppm, 2807 ppm, 3160 ppm, and 3612 ppm for $\text{Hg}(\text{CH}_3)_2$, HgCl_2 , HgBr_2 , and HgI_2 , accordingly, which in percentage amounts to $\sim 58\% \Rightarrow 45\%$ of the total relativistic corrections for the $\text{Hg}(\text{CH}_3)_2 \Rightarrow \text{HgI}_2$ series at the DFT/BP86 level. ZORA estimates relativistic corrections of 1845 ppm, 2745 ppm, 3984 ppm, and 5394 ppm for $\text{Hg}(\text{CH}_3)_2$, HgCl_2 , HgBr_2 and HgI_2 , accordingly, which in percentage amounts to $\sim 47\% \Rightarrow 72\%$ of the total relativistic corrections. However, even though

ZORA underestimates Hg NMR shielding constants by ~ 2100 ppm, the differences between Hg chemical shift values obtained using ZORA and four-component approaches (without spin-density contribution to the XC kernel) are less than 60 ppm and are similar for all three compounds as shown in Table VII and Fig. 1. This is in a good agreement with the conclusion made by Autschbach⁸⁶ that ZORA is a reliable tool for the investigation of chemical shifts as a “valence” property due to very accurate hyperfine integrals for the valence shells of heavy atoms in contrast to inner-most core shells which are important for shielding constants.

In order to evaluate SO contribution to Hg shielding constants and chemical shifts in HgL_2 ($L = \text{Cl}, \text{Br}, \text{I}$) compounds and understand why LR-ESC does not reproduce the Hg chemical shift trend with increasingly heavy halogen ligands, we determined the SO terms in the Hg shielding constants of HgL_2 ($L = \text{CH}_3, \text{Cl}, \text{Br}, \text{I}$) compounds obtained by four-component,⁴ LR-ESC,²⁷ and ZORA (Ref. 18) methods in combination with DFT/BP86 (see Table VIII). Since these methods define the SO terms differently, the direct comparison of SO terms is not possible. Therefore, we present for the HgL_2 ($L = \text{Cl}, \text{Br}, \text{I}$) compounds also the changes from the total Hg shielding constant and SO term values in $\text{Hg}(\text{CH}_3)_2$ (see Table VIII in parenthesis). For HgCl_2 , the change in the SO term (463 ppm), obtained with the four-component approach without spin-density contribution to the XC kernel, corresponds to 23% of the change in total Hg shielding constant value. LR-ESC yields a change of 154 ppm in the SO term and therefore reproduces 33% of the change in SO term obtained with the four-component approach without spin-density contribution to the XC kernel. This underestimation of the change in the SO term accounts for 55% of the difference in the change of the total Hg shielding constant value. The change in SO terms and the contribution to the change in the total Hg shielding constant increases for HgBr_2

TABLE VIII. SO terms and the total values of Hg shielding constants of HgL_2 ($L = \text{CH}_3, \text{Cl}, \text{Br}, \text{I}$) compounds (in ppm) calculated using LR-ESC, ZORA, and four-component approaches (without and with spin-density contribution to the XC kernel) in combination with DFT/BP86. In parenthesis we present the changes from the total Hg shielding constant and SO term values in $\text{Hg}(\text{CH}_3)_2$. The SO term in the four-component approach (without and with spin-density contribution to the XC kernel) was calculated as the difference between Hg shielding constant value calculated including SO contribution and Hg shielding constant value calculated using spin-free formalism.

Molecule	N	LR-ESC		ZORA		Four-component		Four-component spin-density	
		SO	Total	SO	Total	SO	Total	SO	Total
$\text{Hg}(\text{CH}_3)_2$	Hg	-434	8533	2906	7967	-1197	10 015	-953	10 276
HgCl_2	Hg	-280 (154)	10 010 (1477)	3217 (311)	9948 (1981)	-734 (463)	12 049 (2034)	-494 (459)	12 306 (2030)
HgBr_2	Hg	19 (453)	10 355 (1822)	4410 (1504)	11 179 (3212)	387 (1584)	13 254 (3239)	806 (1759)	13 691 (3415)
HgI_2	Hg	467 (901)	10403 (1870)	5882 (2976)	12 185 (4218)	1743 (2940)	14 265 (4250)	2305 (3258)	14 845 (4569)

(1584 ppm and 49%) and even more for HgI_2 (2940 ppm and 69%) when using the four-component method without spin-density contribution to the XC kernel. Here, ZORA yields a very similar trend with 1504 ppm and 47% for HgBr_2 and 2976 ppm and 71% for HgI_2 . For HgBr_2 , ZORA reproduces 95% of the change in SO term obtained with the four-component approach without spin-density contribution to the XC kernel, whereas for HgI_2 it overestimates it by $\sim 1.2\%$. Therefore, the differences between Hg chemical shift values obtained using the ZORA and four-component approaches without spin-density contribution to the XC kernel are less than 60 ppm for all compounds, whereas LR-ESC underestimates the change in the SO term (453 ppm and 901 ppm) and reproduces only 29% and 31% of the change in SO term obtained with the four-component approach without spin-density contribution to the XC kernel for HgBr_2 and HgI_2 , respectively. The underestimation of the change in SO term accounts for 80% and 86% of the difference in the change of the total Hg shielding constant value for HgBr_2 and HgI_2 , respectively. Consequently, one can conclude that underestimation of the SO term is one of the main reasons why LR-ESC does not reproduce the trend in the Hg chemical shifts with increasingly heavy halogen ligands, but it is not the only reason.

All the DFT based four-component results discussed so far did not include spin-density contributions to the XC kernel in the calculations of the shielding constant. The impact of non-collinear spin-density contribution to the XC kernel on $\sigma(N)$ ($N = \text{Hg}, \text{C}, \text{Cl}, \text{Br}, \text{I}$) shielding constants and $\delta(^{199}\text{Hg})$ chemical shifts in fully relativistic four-component calculations at the level of DFT/BP86 is presented in Table VII, in parenthesis under (*spin-density*) and in Fig. 1 as *Four-component spin-density*. While the C shielding constant is reduced by 5 ppm (3%) due to the non-collinear spin-density contribution, Cl shielding constant remains unaffected and Br and I shielding constants increase by 23 ppm (0.9%) and 81 ppm (1.5%), respectively. Within the series of halogen compounds, including non-collinear spin-density contribution gives rise to an increase of the Hg shielding constants and chemical shifts. Hg shielding constant values are increased by 261 ppm (2.6%), 257 ppm (2.1%), 437 ppm (3.3%), and 1581 ppm (4.1%) for $\text{Hg}(\text{CH}_3)_2$, HgCl_2 , HgBr_2 , and HgI_2 , respectively. These changes are primarily due to the changes in SO terms as shown in Table VIII. Whereas Hg chemical shift in HgCl_2

is almost unaffected by non-collinear spin-density contribution (non-collinear spin-density effects on Hg shielding constants of $\text{Hg}(\text{CH}_3)_2$ and HgCl_2 cancel out), Hg chemical shifts in the heavier halogen compounds HgBr_2 and HgI_2 are reduced by 179 ppm (5.5%) and 325 ppm (7.5%). From this we conclude that Hg chemical shifts determined by the ZORA method agree very well with four-component/spin-density results for HgCl_2 , whereas larger deviations (up to 366 ppm) occur for Hg chemical shifts in HgBr_2 and HgI_2 .

B. HF versus DFT

In this section results from HF calculations are compared with DFT calculations using three different functionals, GGA/BP86 and hybrids B3LYP (20% HF exchange) and PBE0 (25% HF exchange). In general, DFT reduces the shielding constants of all atoms and Hg chemical shifts compared to HF in LR-ESC and four-component calculations. The conclusion that DFT gives lower shielding constants compared to HF has been reported previously (e.g., in Ref. 87–90). In addition, hybrid functionals containing exact HF exchange lead to smaller reductions compared to GGA/BP86 and therefore give results which are in better agreement with HF, especially PBE0 which has a larger percentage of HF exchange than B3LYP. Furthermore, we observe that the differences between HF and DFT results increase with a more accurate treatment of relativistic corrections. The largest differences are thus observed in the four-component calculations. Finally, the calculated Hg chemical shifts using different functionals are similar in four-component and ZORA calculations.

C. Shielding tensor elements and their relation to molecular structure and charge distribution

Obviously the isotropic shielding does not describe differences in individual tensor elements, nor differences between individual elements in a series of coordination compounds. Thus, it is conceivable that the same isotropic shielding is observed for two different molecules, despite the fact that the individual tensor elements are quite different, although this is not the case for the linear molecules investigated in this work. In Table IX the full shielding tensor in terms of components parallel and perpendicular to the molecular symmetry axis is presented for the four test

TABLE IX. Components of the total Hg shielding tensor (perpendicular $\sigma_{\perp}(^{199}\text{Hg})$ and parallel $\sigma_{\parallel}(^{199}\text{Hg})$ to the molecular symmetry axis) and isotropic shielding constants $\sigma(^{199}\text{Hg})$ calculated with the four-component approach at the level of DFT/BP86 including non-collinear spin-density contribution to the XC kernel and with the gauge origin placed at Hg.

Molecule	$\sigma_{\perp}(^{199}\text{Hg})$	$\sigma_{\parallel}(^{199}\text{Hg})$	$\sigma(^{199}\text{Hg})$
Hg(II)	16 053	16 053	16 053
Hg(CH ₃) ₂	7167	16 492	10 276
HgCl ₂	10 381	16 157	12 306
HgBr ₂	12 473	16 128	13 691
HgI ₂	14 483	15 569	14 845

molecules. As expected for a linear molecule, the anisotropy, i.e., the difference between the parallel and the perpendicular component, is high for Hg(CH₃)₂. The anisotropy decreases down the series HgCl₂ → HgBr₂ → HgI₂. This correlates with the molecular electric quadrupole moment (see Table II in supplementary material⁸⁰), which is small for HgI₂, indicating that the charge distribution for this molecule is almost spherical. As such, this series of test molecules covers three important features of mercury containing compounds: (1) a systematic change from linear to almost spherical charge density, (2) a systematic increase in the atomic number of the ligand, and (3) both ionic and covalent Hg–ligand bonds are represented. Thus, the results presented in this work might be transferable to a broader selection of mercury containing molecules.

It is noteworthy that the parallel component of the shielding tensor is almost the same as that determined for Hg(II) ion. In a simple picture, this may be understood as the external magnetic field inducing a current around the symmetry axis of the molecule, which is similar to that induced in Hg(II) ion, whereas the induced current in the plane in which the co-

ordinating atom lies is hindered, leading to smaller values of the shielding tensor.

D. Comparison with experimental data and other theoretical studies

In Table X other theoretical studies as well as experimental data are compiled for the four test molecules. Comparing the results in this work (four-component and ZORA) with the experimental data, the qualitative trends are the same, but there are large systematic quantitative differences amounting to up to ~1000 ppm. These differences are even larger if we include the non-collinear spin-density contribution to the XC kernel in the four-component calculations. The use of hybrid functionals, B3LYP and especially PBE0, gives larger Hg chemical shift values by up to ~300 ppm compared to the GGA/BP86 functional, and therefore, results in better correspondence with the experimental values. The differences between calculated and experimental values are expected because (1) rovibrational effects on the shielding constant are not included in the calculation, and probably more importantly, (2) the calculations are carried out in the gas phase, whereas the experiments are carried out in various solvents.^{91–93} The linear geometries of mercury compounds were determined with electron diffraction studies in the gas phase and it was shown that they are bent in solution as the halide–Hg–halide bond angle decreases, as one chooses solvents with higher ability to coordinate to mercury.^{94,95} For example, in DMSO the halide–Hg–halide angle was determined to be 162°, 158°, and 156° with Hg–halide bond distances 2.32 Å, 2.455 Å, and 2.625 Å (Ref. 96) for HgCl₂, HgBr₂, and HgI₂, respectively. Consequently, the coordination of solvent molecules to mercury changes the chemical shifts, $\delta(^{199}\text{Hg})$.^{91,92} Wolff *et al.*¹⁸ showed that a change in 0.01 Å in bond-length leads to ~50 ppm change in calculated

TABLE X. Shielding constants, $\sigma(\text{Hg})$, and chemical shifts, $\delta(^{199}\text{Hg})$, of HgL₂ (L = CH₃, Cl, Br, I) compounds (in ppm) reported in the literature are compared to values calculated in this work. The Hg chemical shift is calculated as $\delta(^{199}\text{Hg}_{\text{HgL}_2}) = (\sigma(^{199}\text{Hg}_{\text{Hg(CH}_3)_2}) - \sigma(^{199}\text{Hg}_{\text{HgL}_2})) / (1 - \sigma(^{199}\text{Hg}_{\text{Hg(CH}_3)_2}))$, with shielding constants obtained in this work, ZORA (Ref. 18) and FP-QR (Ref. 24) studies.

Molecule	Calculated							Experimental ^a					
	Four-component spin-density		Four-component			ZORA	ZORA ^b	SO-UHF ^c	FP-QR ^d	Water	THF	DMSO	Pyridine
	BP86		BP86	B3LYP	PBE0	BP86	Ref. [18]	Ref. [31]	Ref. [24]	Ref. [93]	Ref. [92]	Ref. [92]	Ref. [92]
Shielding constants, $\sigma(^{199}\text{Hg})$													
Hg(CH ₃) ₂	10 276		10 015	10 381	10 536	7967	8019.9		12 772.2				
HgCl ₂	12 306		12 049	12 353	12 443	9948	9575.9	10 908	13 940.0				
HgBr ₂	13 691		13 254	13 528	13 526	11 179	10 704.4	13 523	16 234.3				
HgI ₂	14 845		14 265	14 561	14 496	12 185	11 526.0	14 943	17 551.6				
Chemical shifts, $\delta(^{199}\text{Hg})$													
HgCl ₂	−2051		−2055	−1992	−1927	−1996	−1568.5		−1182.9	−1590.0	−1518.6	−1498.8	−1279.5
HgBr ₂	−3450		−3271	−3180	−3021	−3237	−2706.2		−3506.8		−2213.1	−2062.1	−1622.2
HgI ₂	−4617		−4292	−4223	−4002	−4251	−3534.4		−4841.2		−3447.0	−3119.0	−2355.1

^aExperimental $\delta(^{199}\text{Hg})$ chemical shift values were determined in water, THF, DMSO, and pyridine.

^bZORA results are obtained by Wolff *et al.* (Ref. 18) using ADF package, PW91 functional, and TZ2P basis set with frozen cores.

^cSO-UHF represents a combination of relativistic spin-free no-pair theory of Sucher and Hess and the spin-orbit unrestricted HF, which was employed by Nakatsuji *et al.* (Ref. 31). The results presented here were obtained using a relativistic hamiltonian (free particle) including spin-orbit effects.

^dFP-QR (full name: GIAO-FP-QR-GUHF) method stands for the GIAO method for the finite perturbation theory and the GUHF wave function in combination with the QR-2 approximation was employed by Fukuda *et al.* (Ref. 24).

Hg chemical shift of HgCl_2 , whereas every 10° change in Cl-Hg-Cl angle results in 100 ppm change of Hg chemical shift. According to the experiments from Refs. 93–95, the coordinating ability increases in the order $\text{water} \simeq \text{THF} < \text{DMSO} < \text{pyridine}$. This is in good correspondence with the series we observe in Table X. The mercury chemical shifts obtained in the four-component and ZORA calculations are closest to experimental shifts in water and THF and deviate the most from the chemical shifts in pyridine.

Table X also lists the results obtained by other computational studies, such as ZORA by Wolff *et al.*,¹⁸ SO-UHF by Nakatsuji *et al.*,³¹ and GIAO-Finite Perturbation-quasirelativistic-generalized unrestricted Hartree-Fock (GIAO-FP-QR-GUHF) by Fukuda *et al.*²⁴ The ZORA calculations reported in Wolff *et al.* differ in several aspects from those presented in this work, such as DFT functional (BP86 versus PW91, which does not have a big influence: changes of 2–19 ppm for the Hg shielding constant in all four compounds were calculated using the QZ4P basis set and Gaussian/point nucleus models), and more notably different basis sets (QZ4P all-electron versus TZ2P frozen core). As demonstrated in Sec. III, using the TZ2P basis set, in contrast to QZ4P, gives an error of ~ 400 ppm for Hg shielding constant in HgCl_2 , accounting for most of the differences between the results of Wolff *et al.*¹⁸ and the results presented in this work. Since TZ2P and QZ4P basis sets give similar Hg shielding constant values in $\text{Hg}(\text{CH}_3)_2$, contrary to HgCl_2 , HgBr_2 , and HgI_2 , Hg chemical shifts are also affected by the choice of the basis set by ~ 500 ppm (data not shown). Thus, despite the fact that the results of Wolff *et al.* for the Hg chemical shifts are in better correspondence with experimental shifts, this agreement is probably accidental. Moreover, our ZORA results obtained with the QZ4P basis set are in much better agreement with four-component results.

VI. CONCLUSIONS

We have presented a study of the performance of three different relativistic methods in the calculation of NMR shielding constants and Hg chemical shifts in linear HgL_2 ($L = \text{Cl}, \text{Br}, \text{I}, \text{CH}_3$) compounds. We find that for the C shielding constant both LR-ESC and ZORA reproduce the relativistic corrections and, therefore, the absolute value of the shielding constant obtained by the four-component approach. For Cl and Br these methods behave differently: LR-ESC underestimates the relativistic corrections, whereas ZORA overestimates the relativistic corrections to the shielding constants. For iodine LR-ESC overestimates relativistic corrections, while ZORA even gives the incorrect sign of the relativistic correction. Even though none of the two two-component methods, LR-ESC and ZORA, can reproduce relativistic corrections to the absolute shielding constants of mercury, ZORA reproduces the trend of relative relativistic corrections to the Hg shielding constant increasing with the atomic number of the ligand atom, contrary to LR-ESC, partly because the latter underestimates the change in spin-orbit contribution. The differences between Hg chemical shift values obtained using

ZORA and four-component approaches without spin-density contribution to the XC kernel are less than 60 ppm for all compounds using three different functionals, BP86, B3LYP, and PBE0. However, this difference increases up to 213 ppm and 366 ppm for HgBr_2 and HgI_2 , respectively, if we compare with four-component calculations with non-collinear spin-density contribution to the XC kernel. However, we have investigated only linear mercury compounds and further studies would be necessary in order to test more generally that ZORA can be used as an alternative to the computationally demanding four-component approach for calculations of heavy atom chemical shifts. We have also shown that DFT reduces the shielding constants of all atoms and Hg chemical shifts compared to HF in LR-ESC and four-component calculations. It is noteworthy that hybrid functionals (B3LYP and PBE0) containing HF exchange lead to smaller reductions compared to GGA/BP86 and, therefore, results in better agreement with HF results. We have also found that the four-component method exhibits better basis set convergence than ZORA and LR-ESC methods. Moreover, we have investigated the effect on the Hg shielding constants and Hg chemical shifts of using a finite nucleus model in the form of a Gaussian charge distribution for the Coulomb potential of the nuclei and found that the effect is larger in four-component calculations compared to ZORA and increases with the atomic number of the coordinating atom.

ACKNOWLEDGMENTS

J.I.M. is a member of CONICET (Consejo Nacional de Investigaciones Científicas y Técnicas, Argentina) and acknowledges financial support from Grants CONICET (PIP 5119/05). S.P.A.S. acknowledges support by grants from the Danish Natural Science Research Council/Danish Councils for Independent Research (Grant No. 272-08-0486) and the Carlsberg foundation. L.H. acknowledges the Danish Natural Science Research Council/Danish Councils for Independent Research (Grant No. 272-07-0619) for financial support. The authors thank the Danish Center for Scientific Computing (DCSC) for the computational resources. The authors are grateful to Jochen Autschbach, Trond Saue, Erik van Lenthe, Ken Dyall, Radovan Bast, Alejandro Maldonado, and Perttu Lantto for helpful discussions.

¹L. M. Utschig, J. W. Bryson, and T. V. O'Halloran, *Science* **268**, 380 (1995).

²O. Irazzo, P. W. Thulstrup, S. Ryu, L. Hemmingsen, and V. L. Pecoraro, *Chem. Eur. J.* **13**, 9178 (2007).

³M. Łuczowski, M. Stachura, V. Schirf, B. Demeler, L. Hemmingsen, and V. L. Pecoraro, *Inorg. Chem.* **47**, 10875 (2008).

⁴L. Visscher, T. Enevoldsen, T. Saue, H. J. Aa. Jensen, and J. Oddershede, *J. Comput. Chem.* **20**, 1262 (1999).

⁵S. S. Gomez, R. H. Romero, and G. A. Aucar, *J. Chem. Phys.* **117**, 7942 (2002).

⁶J. Vaara and P. Pyykkö, *J. Chem. Phys.* **118**, 2973 (2003).

⁷P. Lantto, R. H. Romero, S. S. Gomez, G. A. Aucar, and J. Vaara, *J. Chem. Phys.* **125**, 184113 (2006).

⁸M. Iliaš, T. Saue, T. Enevoldsen, and H. J. Aa. Jensen, *J. Chem. Phys.* **131**, 124119 (2009).

⁹I. P. Grant and H. M. Quiney, *Int. J. Quantum Chem.* **80**, 283 (2000).

¹⁰L. Visscher, O. Visser, P. J.C. Aerts, H. Merenga, and W. C. Nieuwpoort, *Comput. Phys. Commun.* **81**, 120 (1994).

- ¹¹L. Cheng, Y. Xiao, and W. Liu, *J. Chem. Phys.* **131**, 244113 (2009).
- ¹²S. Komorovský, M. Repiský, O. L. Malkina, V. G. Malkin, I. M. Ondik, and M. Kaupp, *J. Chem. Phys.* **128**, 104101 (2008).
- ¹³S. Komorovský, M. Repiský, O. L. Malkina, and V. G. Malkin, *J. Chem. Phys.* **132**, 154101 (2010).
- ¹⁴C. Chang, M. Pelissier, and P. Durand, *Phys. Scr.* **34**, 394 (1986).
- ¹⁵E. van Lenthe, E. J. Baerends, and J. G. Snijders, *J. Chem. Phys.* **99**, 4597 (1993).
- ¹⁶E. van Lenthe, E. J. Baerends, and J. G. Snijders, *J. Chem. Phys.* **101**, 9783 (1994).
- ¹⁷E. van Lenthe, J. G. Snijders, and E. J. Baerends, *J. Chem. Phys.* **105**, 6505 (1996).
- ¹⁸S. K. Wolff, T. Ziegler, E. van Lenthe, and E. J. Baerends, *J. Chem. Phys.* **110**, 7689 (1999).
- ¹⁹M. Iliaš and T. Saue, *J. Chem. Phys.* **126**, 064102 (2007).
- ²⁰Q. Sun, W. Liu, Y. Xiao, and L. Cheng, *J. Chem. Phys.* **131**, 081101 (2009).
- ²¹K. Kudo and H. Fukui, *J. Chem. Phys.* **123**, 114102 (2005).
- ²²K. Kudo and H. Fukui, *J. Chem. Phys.* **124**, 209901 (2006).
- ²³R. Fukuda, M. Hada, and H. Nakatsuji, *J. Chem. Phys.* **118**, 1015 (2003).
- ²⁴R. Fukuda, M. Hada, and H. Nakatsuji, *J. Chem. Phys.* **118**, 1027 (2003).
- ²⁵J. Seino and M. Hada, *J. Chem. Phys.* **132**, 174105 (2010).
- ²⁶J. I. Melo, M. C. Ruiz de Azua, C. G. Giribet, G. A. Aucar, and R. H. Romero, *J. Chem. Phys.* **118**, 471 (2003).
- ²⁷J. I. Melo, M. C. Ruiz de Azua, C. G. Giribet, G. A. Aucar, and P. F. Provasi, *J. Chem. Phys.* **121**, 6798 (2004).
- ²⁸P. Manninen, K. Ruud, P. Lantto, and J. Vaara, *J. Chem. Phys.* **122**, 114107 (2005).
- ²⁹P. Manninen, K. Ruud, P. Lantto, and J. Vaara, *J. Chem. Phys.* **124**, 149901 (2006).
- ³⁰W. Kutzelnigg, *J. Comput. Chem.* **20**, 1199 (1999).
- ³¹H. Nakatsuji, M. Hada, H. Kaneko, and C. C. Ballard, *Chem. Phys. Lett.* **255**, 195 (1996).
- ³²R. E. Taylor, C. T. Carver, R. E. Larsen, O. Dmitrenko, S. Bai, and C. Dybowski, *J. Mol. Struct.* **930**, 99 (2009).
- ³³Y. Ishikawa, T. Nakajima, M. Hada, and H. Nakatsuji, *Chem. Phys. Lett.* **283**, 119 (1998).
- ³⁴J. I. Melo, A. Maldonado, and G. A. Aucar, *Theor. Chem. Acc.* **129**, 483 (2011).
- ³⁵DIRAC, a relativistic *ab initio* electronic structure program, Release DIRAC08 (2008), written by L. Visscher, H. J. Aa. Jensen, and T. Saue, with new contributions from R. Bast, S. Dzubilar, K. G. Dyall, U. Ekström, E. Eliav, T. Fleig, A. S. P. Gomes, T. U. Helgaker, J. Henriksson, M. Iliaš, Ch. R. Jacob, S. Knecht, P. Norman, J. Olsen, M. Pernpointner, K. Ruud, P. Salek, and J. Sikkema (see <http://dirac.chem.sdu.dk>).
- ³⁶DIRAC, a relativistic *ab initio* electronic structure program, Release DIRAC10 (2010), written by T. Saue, L. Visscher, and H. J. Aa. Jensen, with contributions from R. Bast, K. G. Dyall, U. Ekström, E. Eliav, T. Enevoldsen, T. Fleig, A. S. P. Gomes, J. Henriksson, M. Iliaš, Ch. R. Jacob, S. Knecht, H. S. Nataraj, P. Norman, J. Olsen, M. Pernpointner, K. Ruud, B. Schimmelpfennig, J. Sikkema, A. Thorvaldsen, J. Thyssen, S. Villaume, and S. Yamamoto (see <http://dirac.chem.vu.nl>).
- ³⁷DALTON, an *ab initio* electronic structure program, Release 2.0 (2005), see <http://www.daltonprogram.org/>.
- ³⁸Amsterdam Density Functional ADF, Release ADF 2009.01 (2009), written by E. J. Baerends, B. te Velde, and collaborators (Amsterdam) and A. Rauk, T. Ziegler, and collaborators (Calgary) (see <http://www.scm.com>).
- ³⁹A. E. Hansen and T. D. Bouman, *J. Chem. Phys.* **82**, 5035 (1985).
- ⁴⁰P. J. Stephens, F. J. Devlin, C. F. Chabalowski, and M. J. Frisch, *J. Phys. Chem.* **98**, 11623 (1994).
- ⁴¹A. D. Becke, *J. Chem. Phys.* **98**, 5648 (1993).
- ⁴²J. P. Perdew, K. Burke, and M. Ernzerhof, *Phys. Rev. Lett.* **77**, 3865 (1996).
- ⁴³J. P. Perdew, K. Burke, and M. Ernzerhof, *Phys. Rev. Lett.* **78**, 1396 (1996).
- ⁴⁴J. P. Perdew, K. Burke, and Y. Wang, *Phys. Rev. B* **54**, 16533 (1996).
- ⁴⁵C. Adamo and V. J. Barone, *J. Chem. Phys.* **100**, 6158 (1999).
- ⁴⁶A. D. Becke, *Phys. Rev. A* **38**, 3098 (1988).
- ⁴⁷J. P. Perdew, *Phys. Rev. B* **33**, 8822 (1986).
- ⁴⁸J. Jokisaari, S. Järvinen, J. Autschbach, and T. Ziegler, *J. Chem. Phys. A* **106**, 9313 (2002).
- ⁴⁹L. Visscher, *Theor. Chem. Acc.* **98**, 68 (1997).
- ⁵⁰K. G. Dyall and K. Fægri, Jr., *Chem. Phys. Lett.* **174**, 25 (1990).
- ⁵¹R. E. Stanton and S. Havriliak, *J. Chem. Phys.* **81**, 1910 (1984).
- ⁵²M. Pecul, T. Saue, K. Ruud, and A. Rizzo, *J. Chem. Phys.* **121**, 3051 (2004).
- ⁵³L. Visscher, *Adv. Quantum Chem.* **48**, 369 (2005).
- ⁵⁴A. F. Maldonado and G. A. Aucar, *Phys. Chem. Chem. Phys.* **11**, 5615 (2009).
- ⁵⁵K. G. Dyall, *Theor. Chem. Acc.* **112**, 403 (2004).
- ⁵⁶K. G. Dyall, *Theor. Chem. Acc.* **115**, 441 (2006).
- ⁵⁷D. E. Woon and T. H. Dunning, Jr., *J. Chem. Phys.* **98**, 1358 (1993).
- ⁵⁸T. H. Dunning, Jr., *J. Chem. Phys.* **90**, 1007 (1989).
- ⁵⁹L. Visscher and K. G. Dyall, *At. Data Nucl. Data Tables* **67**, 207 (1997).
- ⁶⁰M. C. Ruiz de Azua, J. I. Melo, and C. G. Giribet, *Mol. Phys.* **101**, 3103 (2003).
- ⁶¹D. G. Zaccari, M. C. Ruiz de Azua, J. I. Melo, and C. G. Giribet, *J. Chem. Phys.* **124**, 054103 (2006).
- ⁶²M. Schindler and W. Kutzelnigg, *J. Chem. Phys.* **76**, 1919 (1982).
- ⁶³C. van Wüllen and W. Kutzelnigg, *J. Chem. Phys.* **104**, 2330 (1996).
- ⁶⁴P. Lazzeretti, M. Malagoli, and R. Zanasi, *Chem. Phys. Lett.* **220**, 299 (1994).
- ⁶⁵A. Ligabue, S. P. A. Sauer, and P. Lazzeretti, *J. Chem. Phys.* **118**, 6830 (2003).
- ⁶⁶A. Ligabue, S. P. A. Sauer, and P. Lazzeretti, *J. Chem. Phys.* **126**, 154111 (2007).
- ⁶⁷T. Helgaker and P. Jørgensen, *J. Chem. Phys.* **95**, 2595 (1991).
- ⁶⁸S. K. Wolff and T. Ziegler, *J. Chem. Phys.* **109**, 895 (1998).
- ⁶⁹M. Krykunov, T. Ziegler, and E. van Lenthe, *J. Phys. Chem. A* **113**, 11495 (2009).
- ⁷⁰E. van Lenthe and E. J. Baerends, *J. Comput. Chem.* **24**, 1142 (2003).
- ⁷¹R. Ditchfield, *Mol. Phys.* **27**, 789 (1974).
- ⁷²K. Wolinski, J. F. Hinton, and P. Pullay, *J. Am. Chem. Soc.* **112**, 8251 (1990).
- ⁷³G. Schreckenbach and T. Ziegler, *J. Phys. Chem.* **99**, 606 (1995).
- ⁷⁴K. Kashiwabara, S. Konaka, and M. Kimura, *Bull. Chem. Soc. Jpn.* **46**, 410 (1973).
- ⁷⁵P. A. Akishin, V. P. Spiridonov, and A. N. Khodchenkov, *Zh. Fiz. Khim.* **33**, 20 (1959).
- ⁷⁶V. P. Spiridonov, A. G. Gershikov, and B. S. Butayev, *J. Mol. Struct.* **52**, 53 (1979).
- ⁷⁷K. Kashiwabara, S. Konaka, T. Iijima, and M. Kimura, *Bull. Chem. Soc. Jpn.* **46**, 407 (1973).
- ⁷⁸T. Kupka, *Magn. Reson. Chem.* **46**, 851 (2008).
- ⁷⁹T. Kupka, *Magn. Reson. Chem.* **47**, 210 (2009).
- ⁸⁰See supplementary material at <http://dx.doi.org/10.1063/1.3608153> for additionally constructed ADF basis sets and calculated atomic charges and molecular quadrupole moments of linear HgL₂ (L = Cl, Br, I, CH₃) compounds.
- ⁸¹E. Malkin, I. Malkin, O. L. Malkina, V. G. Malkin, and M. Kaupp, *Phys. Chem. Chem. Phys.* **8**, 4079 (2006).
- ⁸²E. Malkin, M. Repisky, S. Komorovský, P. Mach, O. L. Malkina, and V. G. Malkin, *J. Chem. Phys.* **134**, 044111 (2011).
- ⁸³U. Edlund, T. Lejon, P. Pyykkö, T. K. Venkatchalam, and E. Buncel, *J. Am. Chem. Soc.* **109**, 5982 (1987).
- ⁸⁴C. J. Jameson and J. Mason, *Multinuclear NMR*, edited by J. Mason (Plenum, New York, 1987).
- ⁸⁵M. Kaupp, *Theoretical and Computational Chemistry. Relativistic Electronic Structure Theory, Part 2: Applications*, edited by P. Schwerdtfeger, Vol. 14 (Elsevier B.V., Amsterdam, 2004).
- ⁸⁶J. Autschbach, *Theor. Chem. Acc.* **112**, 52 (2004).
- ⁸⁷M. Bühl, M. Kaupp, O. L. Malkina, and V. G. Malkin, *J. Comput. Chem.* **20**, 91 (1999).
- ⁸⁸L. K. Sanders and E. Oldfield, *J. Phys. Chem. A* **105**, 8098 (2001).
- ⁸⁹A. A. Auer, J. Gauss, and J. F. Stanton, *J. Chem. Phys.* **118**, 10407 (2003).
- ⁹⁰J. A. Tosell, *Phys. Chem. Miner.* **31**, 41 (2004).
- ⁹¹M. A. Sens, N. K. Wilson, P. D. Ellis, and J. D. Odom, *J. Magn. Reson.* **19**, 323 (1975).
- ⁹²P. Peringer, *Inorg. Chim. Acta* **39**, 67 (1980).
- ⁹³M. Delnomdedieu, D. Georgescauld, A. Boudou, and E. J. Dufourc, *Bull. Magn. Reson.* **11**, 420 (1989).
- ⁹⁴I. Persson, M. Sandström, P. L. Goggin, and A. Mosset, *J. Chem. Soc. Dalton Trans.* 1597 (1985).
- ⁹⁵I. Persson, M. Sandström, and P. L. Goggin, *Inorg. Chim. Acta* **129**, 183 (1987).
- ⁹⁶M. Sandström, *Acta Chem. Scand., Ser. A* **32**, 627 (1978).